
A Model and Sensitivity Analysis of the Quality Economics of Defect-Detection Techniques

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Introduction

Motivation

Problem

Overview

Software Quality

Economics

Example

An Analytical Model

Sensitivity Analysis

Conclusions

Introduction

- Analytical software quality assurance (defect-detection techniques like reviews, tests, ...) is still the most important method to improve the quality of software.
- The costs for those techniques are significant:
 - ◆ Myers (1979) estimates that 50% of the total development costs can be attributed to testing.
 - ◆ Jones (1987) states that 30–40% of the development costs are for quality assurance and defect removal.
 - ◆ The *National Institute of Standards and Technology* (2002) even assigns 80% to the detection and removal of defects.
- There is a huge opportunity for cost savings in that area.

- This results in three questions:
 1. Which techniques should be used?
 2. In what sequence?
 3. With what effort for each technique?
- Ntafos (2001): “Cost is clearly a central factor in any realistic comparison but it is hard to measure, data are not easy to obtain, and little has been done to deal with it.”
- Rai et al. (1998): “A better understanding of the costs and benefits of SQA and improvements to existing quantitative models should be useful to decision-makers.”

Introduction

Motivation

Problem

Overview

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Conclusions

Introduction

Software Quality Economics

Example

An Analytical Model

Sensitivity Analysis

Conclusions

Introduction

**Software Quality
Economics**

Quality Economics

Example

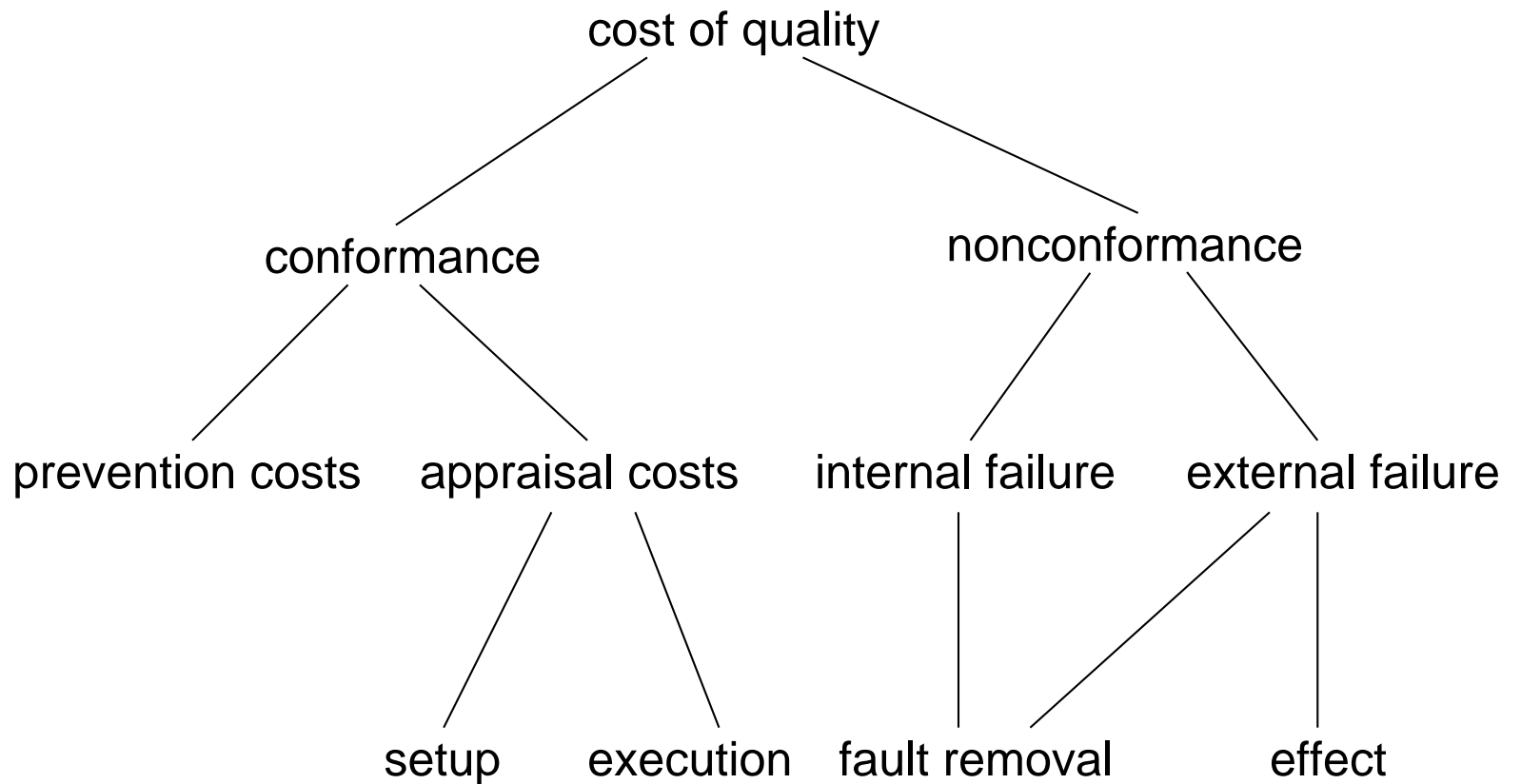
An Analytical Model

Sensitivity Analysis

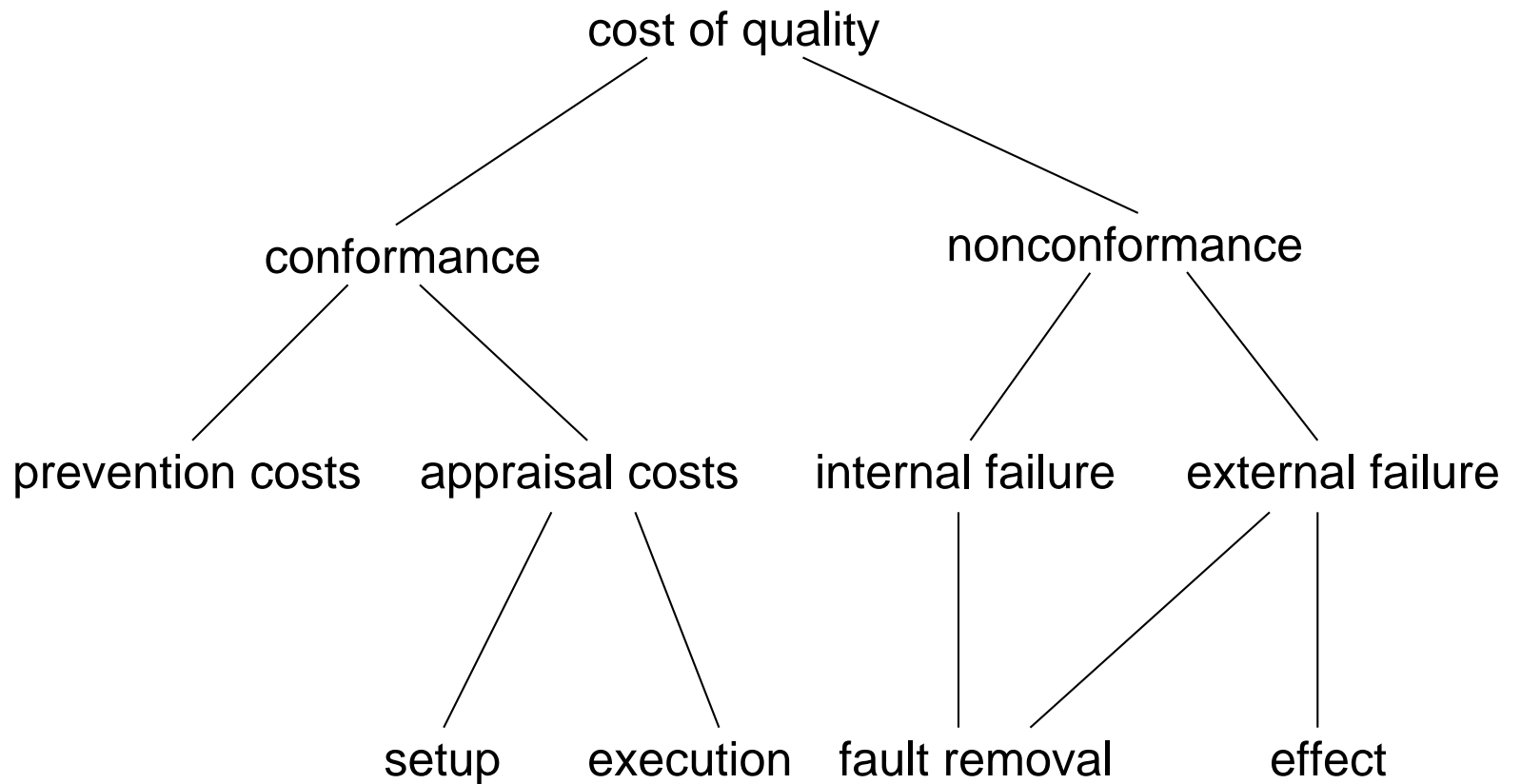
Conclusions

Software Quality Economics

- Quality economics is the cost/benefit analysis w.r.t. quality
- The benefits are the saved costs



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- Focus on *analytical* QA in the following

Introduction

Software Quality
Economics

Example

A Software Project
A Quality Assurance
Plan

An Analytical Model

Sensitivity Analysis

Conclusions

Example

Introduction

Software Quality
Economics

Example

A Software Project

A Quality Assurance
Plan

An Analytical Model

Sensitivity Analysis

Conclusions

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- Maybe some control unit in an automobile
- It consists of 100 KLOC of C code

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- Usually we use the techniques
 - ◆ code inspection (A),
 - ◆ unit test (B),
 - ◆ integration test (C), and
 - ◆ system test (D)

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- Usually we use the techniques
 - ◆ code inspection (A),
 - ◆ unit test (B),
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 - ◆ system test (D)
- *How do you plan the quality assurance?*

Introduction

Software Quality
Economics

Example

A Software Project

**A Quality Assurance
Plan**

An Analytical Model

Sensitivity Analysis

Conclusions

- We expect about 100 defects

Introduction

Software Quality
Economics

Example

A Software Project

A Quality Assurance
Plan

An Analytical Model

Sensitivity Analysis

Conclusions

- We expect about 100 defects
- *What is the best sequence of the techniques? (ABCD or BACD?)*

Introduction

Software Quality
Economics

Example

A Software Project

**A Quality Assurance
Plan**

An Analytical Model

Sensitivity Analysis

Conclusions

- We expect about 100 defects
- *What is the best sequence of the techniques? (ABCD or BACD?)*
- *How much effort is spent on each technique?*
 - ◆ More on the inspection or the unit test?
 - ◆ How much on unit, integration, and system test?

Introduction

Software Quality
Economics

Example

A Software Project
**A Quality Assurance
Plan**

An Analytical Model

Sensitivity Analysis

Conclusions

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- *What does it cost me not to detect and remove some of the defects? (Support, annoyed customers, ...)*
- *How probable is it that they occur at the customer?*

Introduction

Software Quality
Economics

Example

An Analytical Model

General
Difficulty and Defect
Propagation

Example: Direct
Costs

Usage

Example Revisited

Sensitivity Analysis

Conclusions

An Analytical Model

Introduction

Software Quality Economics

Example

An Analytical Model

General

Difficulty and Defect Propagation

Example: Direct Costs

Usage

Example Revisited

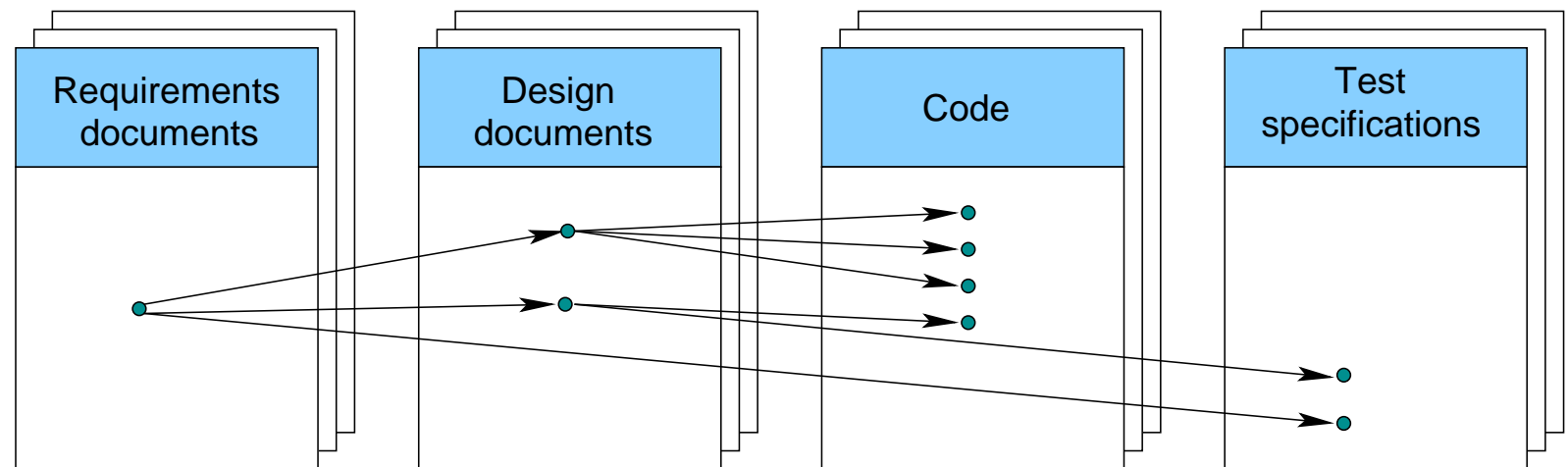
Sensitivity Analysis

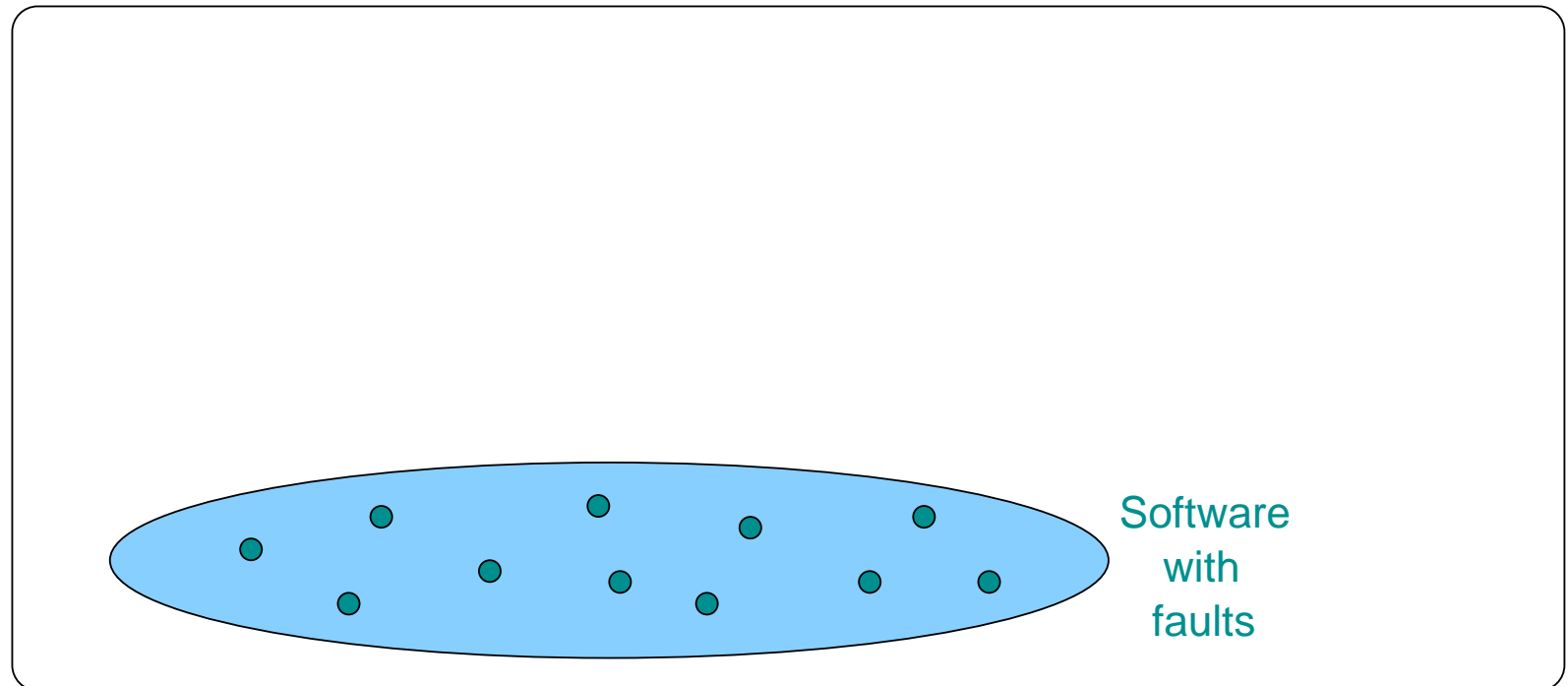
Conclusions

- For all types of defect-detection techniques
- Three components:
 - ◆ Direct costs d_A
 - ◆ Future costs o_A
 - ◆ Revenues / saved costs r_A
- Assumptions:
 - ◆ Found faults are perfectly removed
 - ◆ The effort for a technique can be freely varied
- Not covered:
 - ◆ Time to market
 - ◆ Net present value

- Introduction
- Software Quality Economics
- Example
- An Analytical Model
- General
- Difficulty and Defect Propagation**
- Example: Direct Costs
- Usage
- Example Revisited
- Sensitivity Analysis
- Conclusions

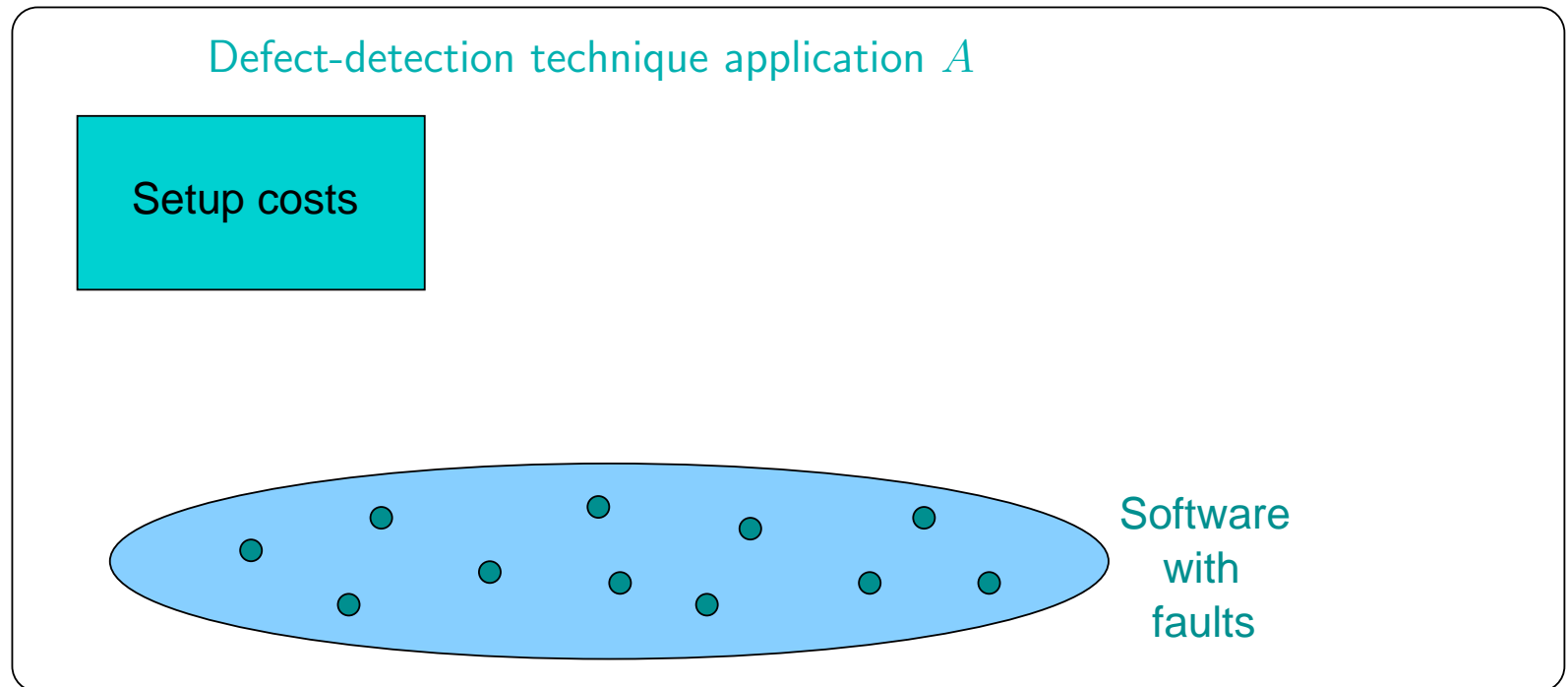
- Difficulty function
 - ◆ Adapted from Littewood et al. (2000)
 - ◆ Describes the probability that a specific defect is not detected by a specific technique
 - ◆ Extended by the dimension *effort*
- Defect propagation





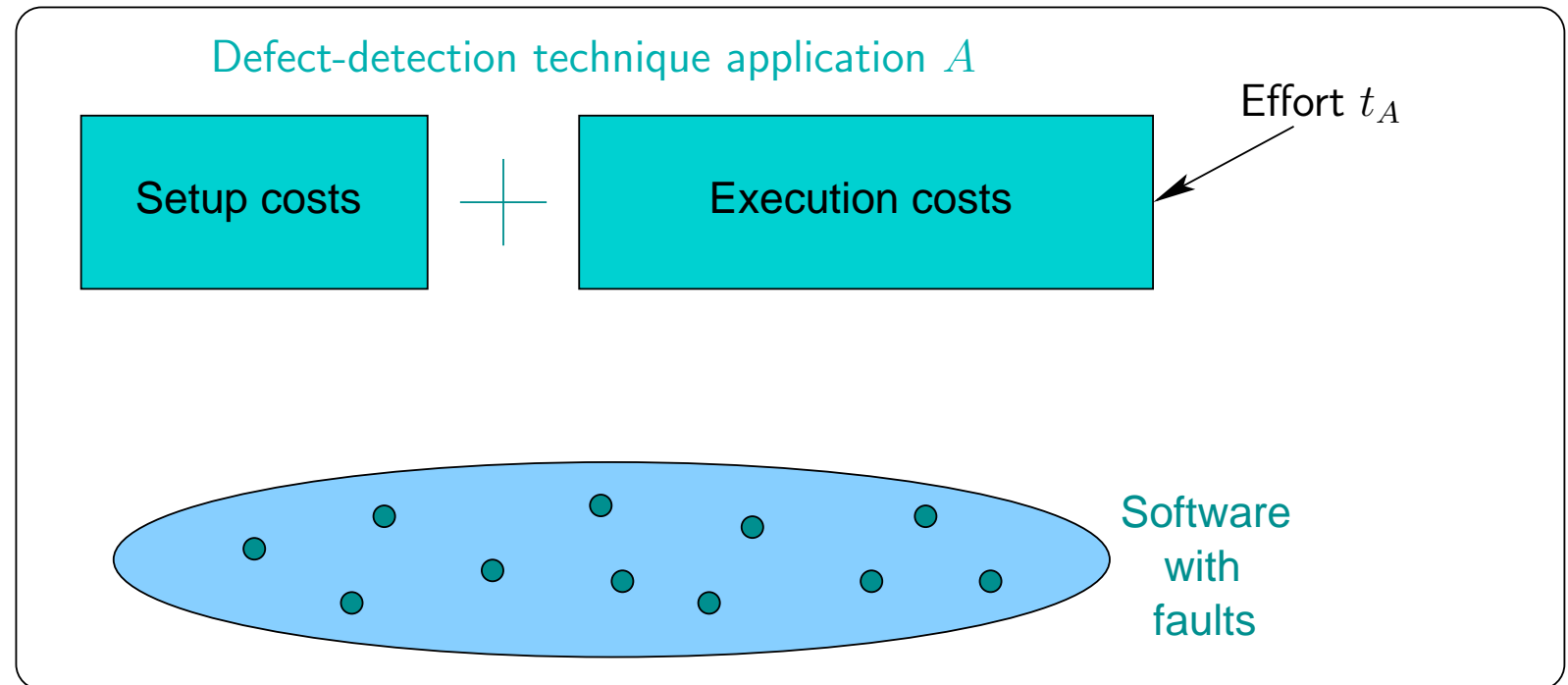
- Costs that can be measured directly from the application of a technique
- Dependent on the effort t

$$d_A = \quad (1)$$



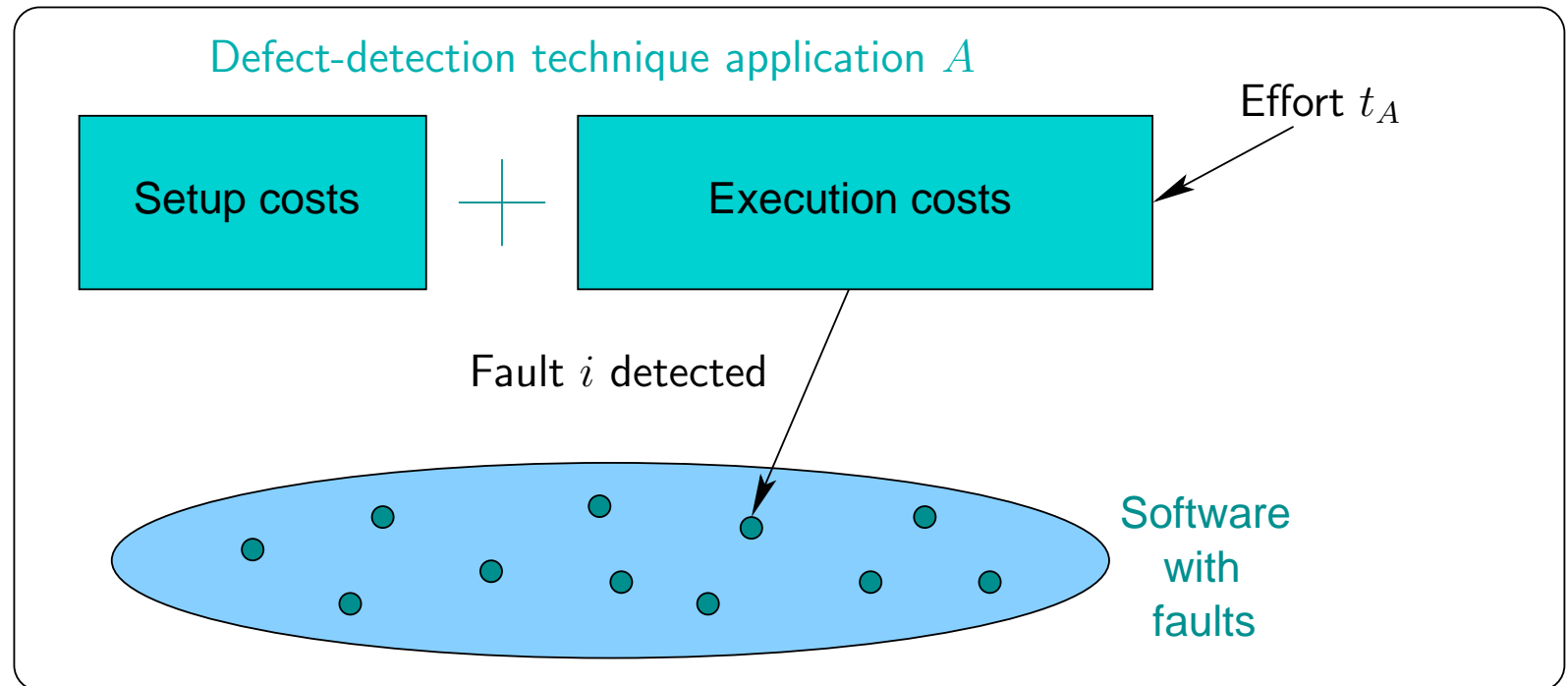
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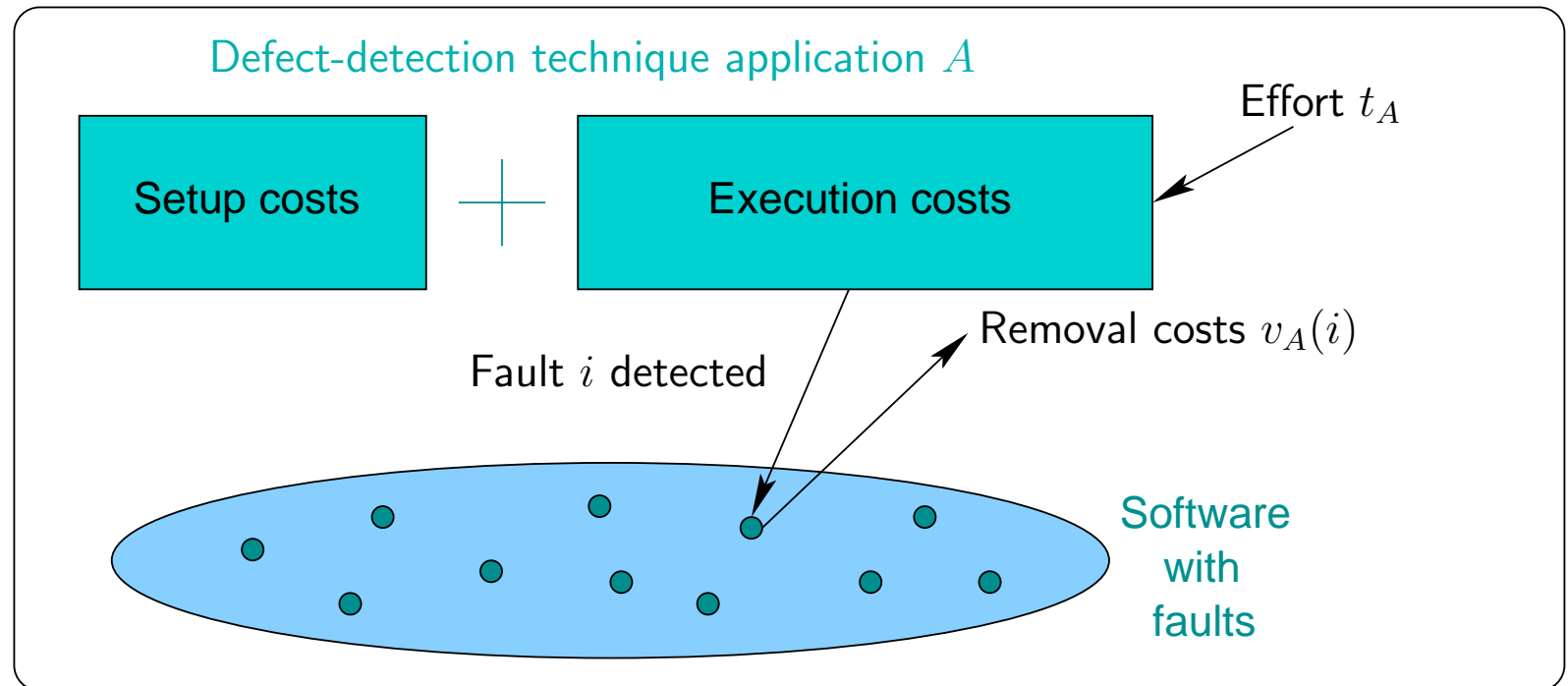
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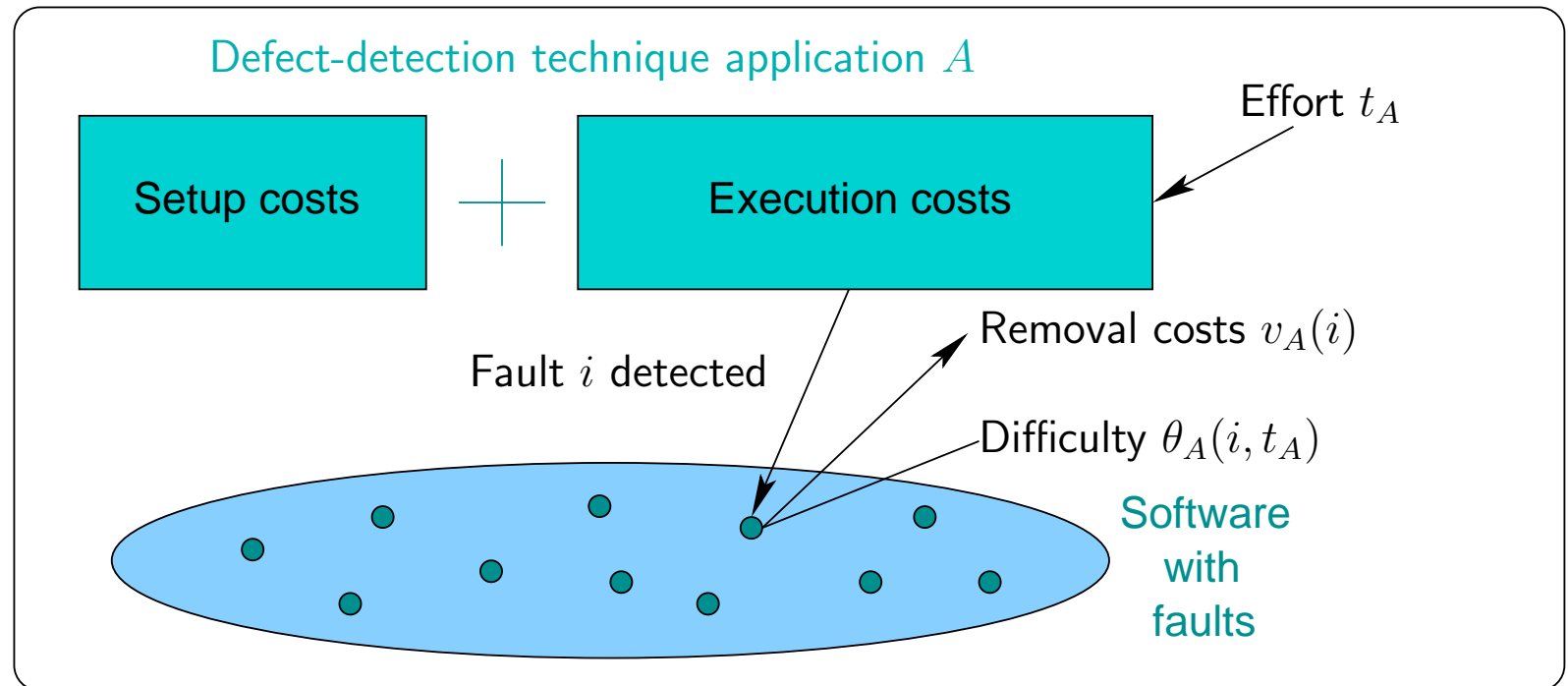
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$$d_A = u_A + e_A(t) + \sum_i (1 - \theta_A(i, t_A))v_A(i) \quad (1)$$

Introduction

Software Quality
Economics

Example

An Analytical Model

General
Difficulty and Defect
Propagation

Example: Direct
Costs

Usage

Example Revisited

Sensitivity Analysis

Conclusions

- Theoretical analysis of defect-detection techniques and improvements
 - ◆ Which parts of the model are affected by improvements?
 - ◆ How do different techniques differ?
 - ◆ What are the most important factors?
- Practical optimisation with simplified model
 - ◆ Grouping of defects by defect types
 - ◆ Collecting data in a company
 - ◆ Predicting for new project based on old data
 - ◆ Using optimisation methods

- Five different effort distributions
- Effort in staff-hours

Dist.	Inspection	Unit test	Int. test	System test	ROI
1	650	300	550	550	0.12
2	0	500	750	750	0.08
3	100	100	100	100	-0.31
4	50	50	50	2000	-0.04
Opt.	800	250	250	200	0.28

Introduction

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Basics

Approach

Results

Conclusions

Sensitivity Analysis

Introduction

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Basics

Approach

Results

Conclusions

- Evaluation of the model w.r.t. the influence of the input factors on the output variance (in our case: ROI)
- Settings: *Factors prioritisation* and *factors fixing*

Introduction

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Basics

Approach

Results

Conclusions

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Introduction

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Basics

Approach

Results

Conclusions

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- Factors fixing
 - ◆ Which factors do *not* cause a significant change to the output variance if their value is fixed to one of their distribution?
 - ◆ Which factors can be removed or fixed to simplify the model and data collection?

Introduction

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Basics

Approach

Results

Conclusions

- Using the FAST method (based on Monte Carlo sampling)
- As implemented in the tool *SimLab*
- Literature review of the available empirical work on the input factors of the model¹.
- From this, the distributions of the input factors were determined.
- Hence, a sensitivity analysis on the basis of found distributions from industry and research

¹Available as Technical Report and will be presented at ISESE '06

- [Introduction](#)
- [Software Quality Economics](#)
- [Example](#)
- [An Analytical Model](#)
- [Sensitivity Analysis](#)
- [Basics](#)
- [Approach](#)
- [Results](#)
- [Conclusions](#)

First order			Total order		
Doc. type	c	0.4698	Doc. type	c	0.8962
Exec. eff.	t	0.1204	Remv. costs f.	v_f	0.4473
Avg. diff.	θ	0.0699	Avg. diff.	θ	0.4255
Remv. costs f.	v_f	0.0541	Setup costs	u	0.3916
Form function	ϕ	0.0365	Exec. eff.	t	0.3859
Setup costs	u	0.0297	Form function	ϕ	0.2888
Remv. costs i.	v	0.0264	Num. of pred.	ρ	0.2711
Num. of pred.	ρ	0.0256	Remv. costs i.	v	0.2546
Failure prob. f.	π	0.0158	Failure prob. f.	π	0.2068
Tech. seq.	s	0.0083	Tech. seq.	s	0.1825
Labour costs	l	0.0010	Labour costs	l	0.1489

- Introduction
- Software Quality Economics
- Example
- An Analytical Model
- Sensitivity Analysis
- Basics
- Approach
- Results**
- Conclusions

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- Other analyses (more differentiated factors, practical model) give only slightly different results

Introduction

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Conclusions

Related Work

Summary

Future work

Conclusions

Introduction

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Conclusions

Related Work

Summary

Future work

- Efficiency models
 - ◆ Often without considering costs and benefits
 - ◆ Only for a specific type of technique
- Economic models
 - ◆ Very abstract
 - ◆ Data collection not clear

[Introduction](#)

[Software Quality Economics](#)

[Example](#)

[An Analytical Model](#)

[Sensitivity Analysis](#)

[Conclusions](#)

[Related Work](#)

[Summary](#)

[Future work](#)

- Costs and benefits are a central factor in planning software quality assurance
- Models of those costs and benefits can help decision makers
- We propose an analytical model of the quality economics
- More detailed as common economical models
- But more general than specific inspection or reliability models
- Sensitivity analysis shows that the removal costs in the field, the document type, the difficulty, and the execution costs have the strongest effects on the output variation

Introduction

Software Quality
Economics

Example

An Analytical Model

Sensitivity Analysis

Conclusions

Related Work

Summary

Future work

- Evaluation of static analysis tools (bug finding tools) using the model with data from a company
- Evaluation of the predictive validity of the model
- Empirical research regarding the most important factors of the model
- Integrated quality modelling and management